

applied field H_z^0 ; and $\Delta H = H_z - H_z^0$. The J_{ij} values are the well-known indirect spin-coupling constants. The D_{ij} values are an average of the direct dipole-dipole interaction over the motion of the molecule in its anisotropic liquid crystal environment.

$$D_{ij} = \gamma_i \gamma_j \frac{\hbar}{2\pi} r_{ij}^{-3} (1 - 3 \cos^2 \theta_{ij}) \quad (2)$$

Here θ_{ij} is the angle between the internuclear vector and the applied field H_z^0 . The internuclear distance is r_{ij} . Because benzene is planar and hexagonal, it may be shown that $(1 - 3 \cos^2 \theta_{ij})$ is the same for all pairs of protons. Thus we anticipate that the D_{ij} will be proportional to r_{ij}^{-3} ; and $D_{meta} = 1/(3\sqrt{3})D_{ortho}$, with $D_{para} = 1/8 D_{ortho}$.

Since the indirect couplings are known to be 10 or less c.p.s.,⁴ the main features of the spectrum are determined by the single constant, D_{ortho} , and the benzene geometry. As is illustrated in Table I, the position of

TABLE I
COMPARISON OF COMPUTED AND EXPERIMENTAL N.M.R.
LINE POSITIONS

Line	Expt., ^a c.p.s.	Computed, ^b c.p.s.			
		I	II	III	IV
A	21.6	20.8	23.9	10.9	20.8
B	55.0	55.6	55.2	54.2	54.5
C	188.8	189.5	189.7	191.4	189.5
D	350.8	349.5	349.0	349.0	350.2
E	431.3	431.1	435.0	432.3	429.1
F	483.6	483.7	484.9	483.6	481.6
G	1019.6	1019.1	1019.1	1019.1	1019.1
H	1091.9	1088.2	1088.5	1089.6	1089.2
I	1203.3	1203.7	1203.7	1203.7	1203.7

^a The experimental line positions are the average from five spectra of the splitting of the high- and low-field lines from the center of the spectrum. ^b In each calculation $D_{ortho} = -639.45$, $D_{meta} = -123.06$, and $D_{para} = -79.93$ c.p.s. In calculation I, $J_{ortho} = +6.0$, $J_{meta} = +2.0$, and $J_{para} = +1.0$ c.p.s. In calculation II, $J_{ortho} = +7.45$, $J_{meta} = +2.0$, and $J_{para} = +1.0$ c.p.s. In calculation III, $J_{ortho} = +6.0$, $J_{meta} = -2.0$, and $J_{para} = +1.0$ c.p.s. In calculation IV, $J_{ortho} = +6.0$, $J_{meta} = +2.0$, and $J_{para} = -1.0$ c.p.s.

the outermost intense line I of Fig. 1 is dependent only on D_{ortho} . Thus by taking $D_{ortho} = \pm 639.45$ c.p.s., all major features of the spectrum may be computer simulated. There are two important exceptions: the lines A are merged at the center of the spectrum, and line E is merged with line D. If J_{ortho} of magnitude 7 c.p.s. and of sign opposite that of D_{ortho} is introduced, then lines A and E move to their experimentally observed regions. If the same sign is employed, A splits correctly, but line E remains under line D. Thus we conclude that the sign of J_{ortho} is opposite to that of D_{ortho} . We have fit the observed spectrum by varying J_{ortho} and giving approximate values having the same sign as J_{ortho} to the smaller indirect interactions J_{meta} and J_{para} . The experimental line positions may be compared with those computed after this fitting, which is calculation I in Table I. All major lines which are not groups of closely overlapping lines have been compared. The variation of J_{ortho} in calculation II moves line E greatly and line A to a lesser degree.

The calculation III shows that a change in sign of J_{meta} moves line A almost 10 c.p.s. Calculation IV shows that the position of most lines is insensitive to the sign of J_{para} ; thus we have nothing to say on its sign now.

A computer-simulated theoretical spectrum with the constants of calculation I of Table I is displayed on the left side of Fig. 1. It is constructed as a sum of Lorentzian lines of half-width at half-height 4.5 c.p.s. It appears that the line width in the experimental spectrum increases from the center to the wings of the spectrum, a phenomenon we attribute to a distribution of liquid crystal domain or swarm¹ orientations with respect to the applied field. Otherwise, the computed relative line intensities are in good agreement with those observed.

We conclude that the Hamiltonian (eq. 1) is adequate to explain the position and relative intensity of the lines in our spectrum. We believe J_{ortho} and J_{meta} have a sign opposite to that of D_{ortho} . If we assume that the planes of dissolved benzene molecules tend to be parallel to those in the liquid crystal molecules and thus parallel to the applied field,¹ then $D_{ortho} = -639.45$ c.p.s., and J_{ortho} and J_{meta} are positive.² We also note that the mean geometry of the protons of benzene must be on the corners of a plane hexagon; otherwise, the assumed relative sizes of D_{meta} and D_{para} would have been incorrect, and major errors in computed relative line positions would have been expected.

It may be shown that $P(\theta, \varphi)$, the probability density per unit solid angle of orientations of the applied field with respect to the sixfold symmetry axis of the benzene, when expanded in real spherical harmonics to $l = 2$, is determined by our observed value of D_{ortho} , which we assume to be negative. Having done this, we obtain eq. 3.

$$P(\theta, \varphi) = 0.10 - 0.05 \cos^2 \theta \quad (3)$$

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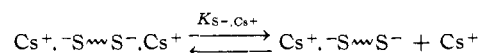
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A Novel Approach to Studies of Triple-Ion Formation

Sir:

It was pointed out by Fuoss¹ that in solvents of a low dielectric constant, free ions may associate with ion pairs into triple ions if the concentration of ion pairs is sufficiently high. Our recent studies of living polystyrene possessing two active ends per chain and Cs^+ as counterion suggested an alternative approach to the problem of triple-ion formation. Dissociation of such a polymer produces a styryl⁻ ion ($\sim\text{S}^-$) linked by a chain to a $\sim\text{S}^-\text{Cs}^+$ ion pair, viz.



(1) R. M. Fuoss and C. A. Krauss, *J. Am. Chem. Soc.*, **55**, 21, 476, 1019, 2387 (1933).